

# Cosmological interpretation for the stochastic signal in pulsar timing arrays

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Based on 2307.00722 (SCPMA), 2307.03141 (SCPMA), 2312.01824 (PRD)

Hunan Normal University

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第五届引力波天体物理研讨会  
暨NSFC引力波天文学创新群体项目交流会



# Outline

## ① Introduction

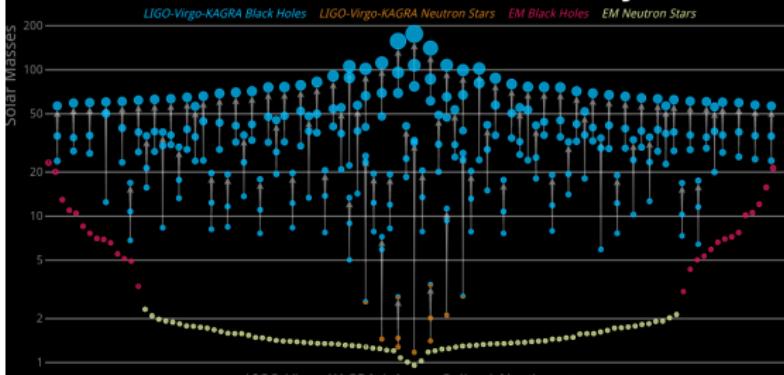
## ② SMBHB

## ③ Cosmological sources

- Phase transition
- Cosmic string
- Scalar-induced GW

## ④ Summary

# Masses in the Stellar Graveyard



Livingston

Hanford

## The Nobel Prize in Physics 2017



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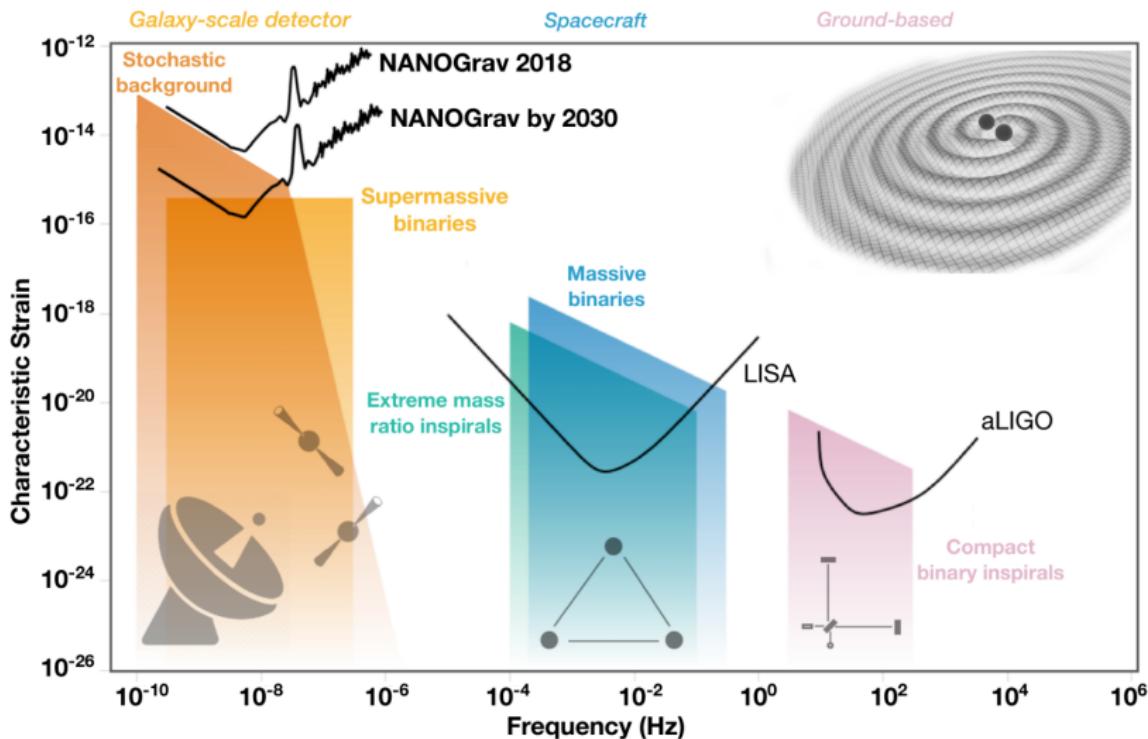


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Barry C. Barish  
Prize share: 1/4



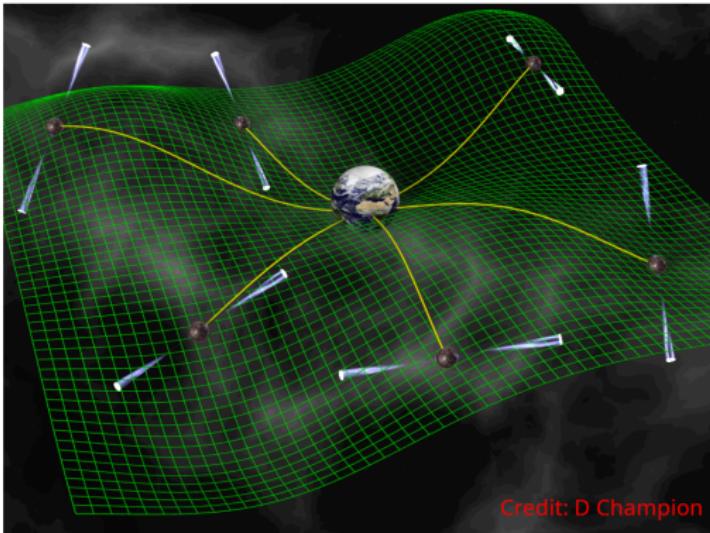
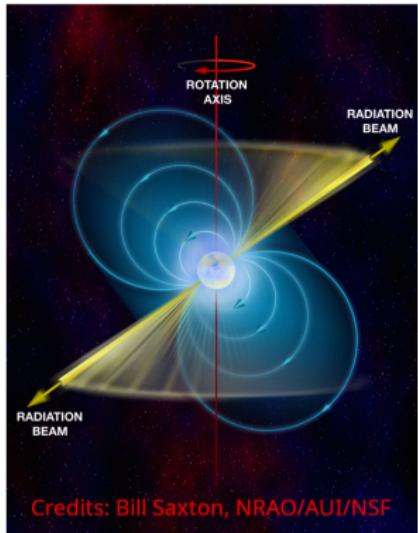
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Elmeled  
Kip S. Thorne  
Prize share: 1/4

- New era of GW astronomy
- Multi-messenger astronomy





# Pulsar and pulsar timing array (PTA)

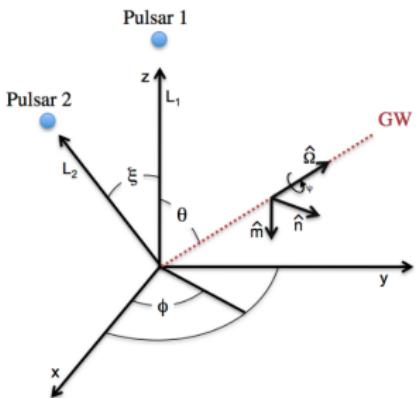


- Pulsars are highly magnetized, rotating neutron stars that emit regular pulses of electromagnetic radiation.
- GWs can cause tiny distortion in spacetime inducing variations in the time of arrivals (ToAs).
- A PTA pursues to detect nHz GWs by regularly monitoring ToAs from an array of the ultra rotational stable millisecond pulsars.



# Timing residual induced by a GWB

- Redshift



$$\begin{aligned} z(t, \hat{\Omega}) &= \frac{\nu_e - \nu_p}{\nu_p} \\ &= \frac{\hat{p}^i \hat{p}^j}{2(1 + \hat{\Omega} \cdot \hat{p})} [h_{ij}(t_p, \hat{\Omega}) - h_{ij}(t_e, \hat{\Omega})] \\ z(t) &= \int_{S^2} d\hat{\Omega} z(t, \hat{\Omega}) \end{aligned}$$

- Timing residual in frequency-domain

$$\tilde{r}(f, \hat{\Omega}) = \frac{1}{2\pi i f} \left( 1 - e^{-2\pi i f L(1 + \hat{\Omega} \cdot \hat{p})} \right) \times \sum_A h_A(f, \hat{\Omega}) F^A(\hat{\Omega})$$

- Antenna pattern

$$F^A(\hat{\Omega}) = e_{ij}^A(\hat{\Omega}) \frac{\hat{p}^i \hat{p}^j}{2(1 + \hat{\Omega} \cdot \hat{p})}$$



# Detecting a GWB with PTA

- Assume the GWB is isotropic, unpolarized, and stationary

$$\left\langle h_A^*(f, \hat{\Omega}) h_{A'}(f', \hat{\Omega}') \right\rangle = \frac{3H_0^2}{32\pi^3 f^3} \delta^2(\hat{\Omega}, \hat{\Omega}') \delta_{AA'} \delta(f - f') \Omega_{\text{gw}}(f)$$

- Spectrum of GWB

$$\Omega_{\text{gw}}(f) \equiv \frac{1}{\rho_{\text{crit}}} \frac{d\rho_{\text{gw}}}{d \ln f}, \quad \rho_{\text{crit}} = \frac{3H_0^2}{8\pi}, \quad \rho_{\text{gw}} = \frac{1}{32\pi} \left\langle \dot{h}_{ij}(t, \vec{x}) \dot{h}^{ij}(t, \vec{x}) \right\rangle,$$

- Cross-power spectral density

$$S_{IJ} = \left\langle \tilde{r}_I^*(f) \tilde{r}_J(f') \right\rangle = \frac{1}{\gamma} \frac{H_0^2}{16\pi^4 f^5} \delta(f - f') \Gamma_{IJ}(f, L_I, L_J, \xi) \Omega_{\text{gw}}(f)$$

- Overlap reduction function (ORF) is function of  $f, L_I, L_J, \xi$

$$\Gamma_{IJ} = \gamma \sum_A \int d\hat{\Omega} \left( e^{2\pi i f L_I (1 + \hat{\Omega} \cdot \hat{p}_I)} - 1 \right) \times \left( e^{-2\pi i f L_J (1 + \hat{\Omega} \cdot \hat{p}_J)} - 1 \right) F_I^A(\hat{\Omega}) F_J^A(\hat{\Omega})$$

- Hellings-Downs correlations for  $fL \gg 1$  (short-wavelength approximation)

$$\Gamma_{IJ} = \frac{3}{2} \left( \frac{1 - \cos \xi}{2} \right) \ln \frac{1 - \cos \xi}{2} - \frac{1 - \cos \xi}{8} + \frac{1}{2}$$

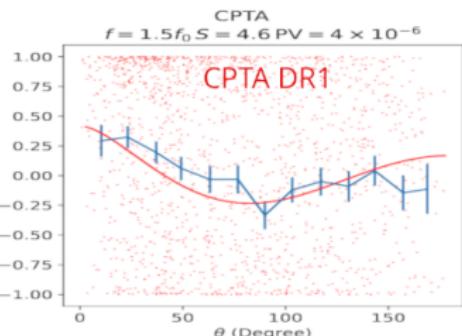
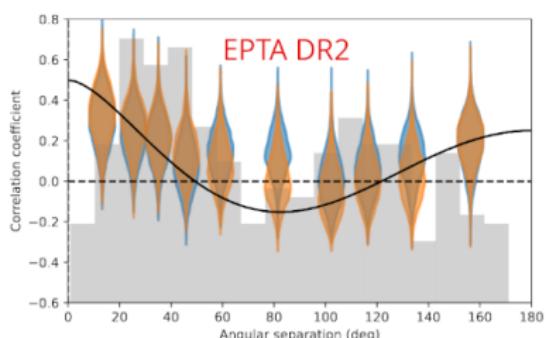
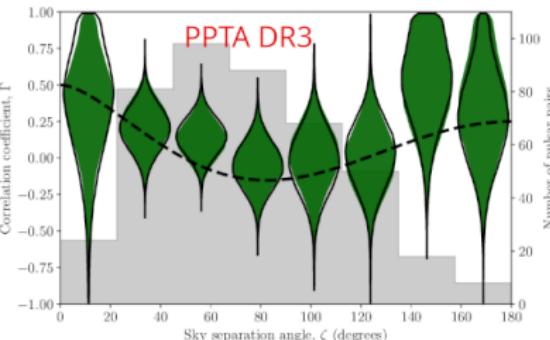
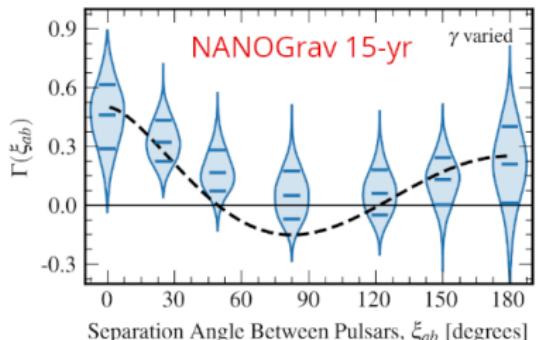


# PTAs in operation





# Evidence for a GWB in PTA data sets



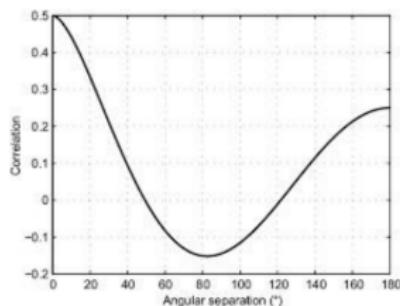
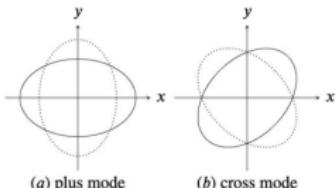
NANOGrav, 2306.16213 (ApJL); PPTA, 2306.16215 (ApJL)

EPTA+InPTA, 2306.16214 (A&A); CPTA, 2306.16216 (RAA)



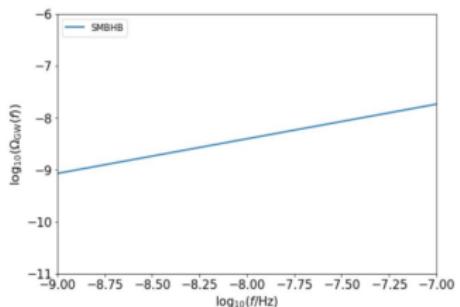
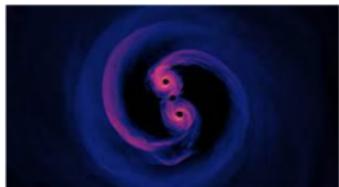
# GWB from SMBHB

$$\langle \tilde{r}_I^*(f) \tilde{r}_J(f') \rangle = \frac{1}{\gamma} \frac{H_0^2}{16\pi^4 f^5} \delta(f - f') \textcolor{red}{\Gamma_{IJ}(f, L_I, L_J, \xi)} \Omega_{\text{gw}}(f)$$



Hellings-Downs curve

$$\begin{aligned}\Gamma_{ab}^{\text{TT}} &= \frac{1}{2} \left[ 1 + \delta_{ab} + 3\kappa_{ab} \left( \ln \kappa_{ab} - \frac{1}{6} \right) \right] \\ \kappa_{ab} &\equiv (1 - \cos \xi_{ab})/2\end{aligned}$$

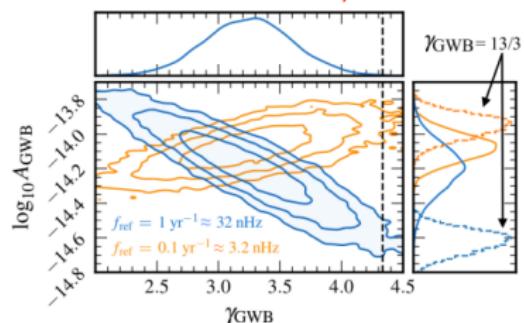


Power law

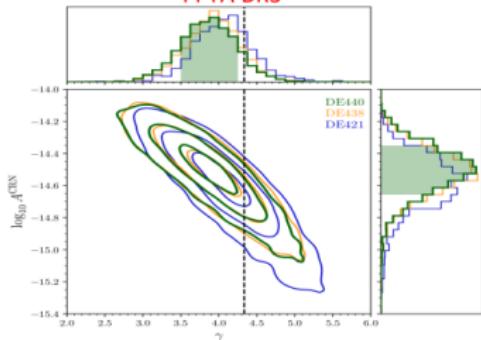
$$\Omega_{\text{gw}}(f) = \frac{2\pi^2 A_{\text{GWB}}^2}{3H_0^2} \left( \frac{f}{f_{\text{yr}}} \right)^{5-\gamma_{\text{GWB}}} f_{\text{yr}}^2$$

$$\gamma_{\text{GWB}} = 13/3$$

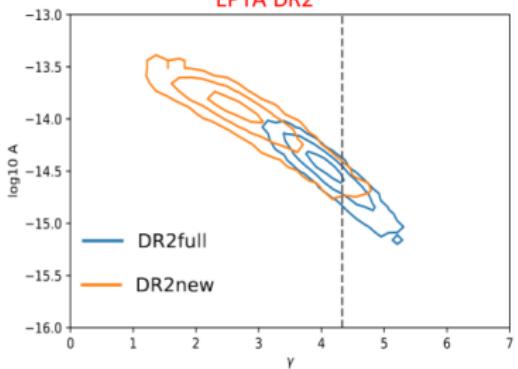
## NANOGrav 15-yr



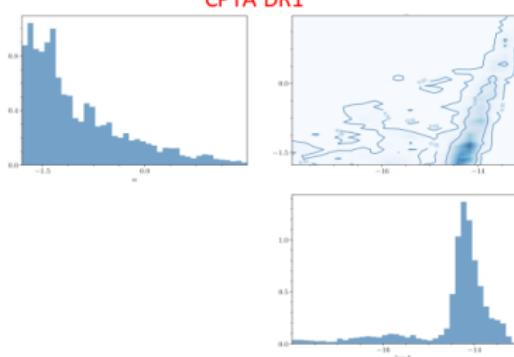
## PPTA DR3



## EPTA DR2



## CPTA DR1

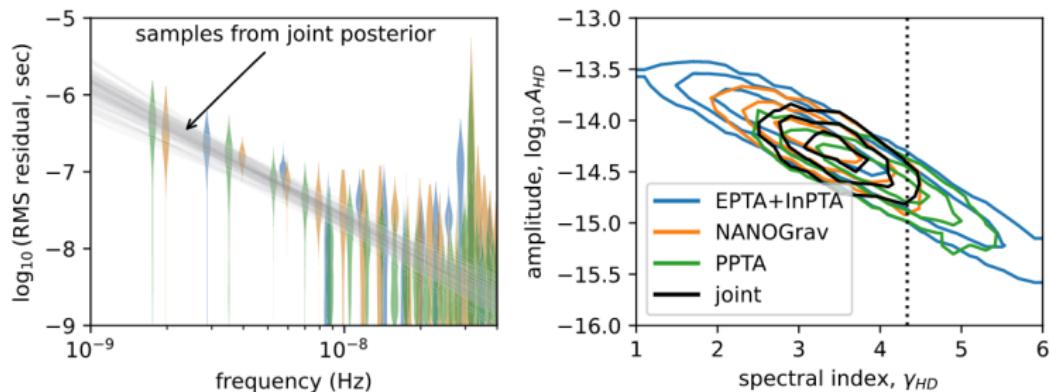


NANOGrav, 2306.16213 (ApJL); PPTA, 2306.16215 (ApJL)

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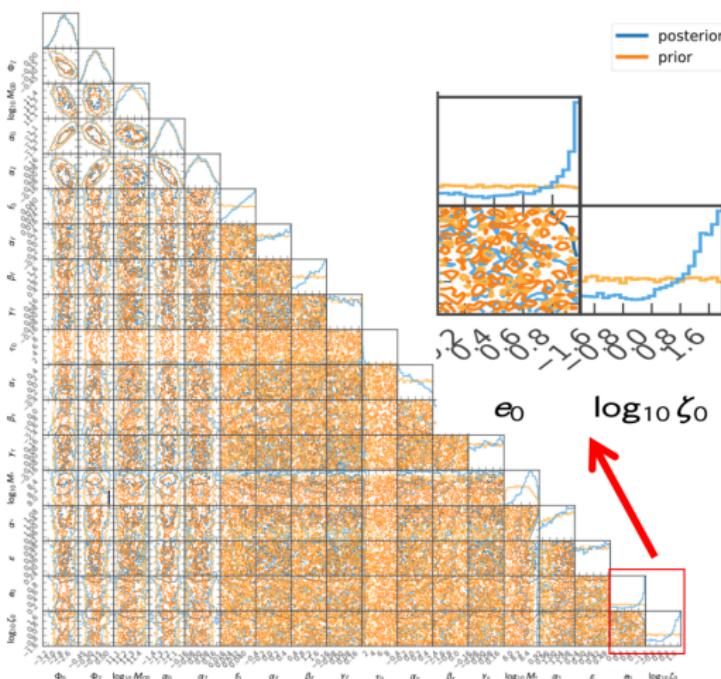
# Comparing results from different PTAs



**Figure 1.** Left: free spectral posteriors for each PTA showing the measured HD-correlated GWB power in several frequency bins under no spectral shape assumption. Each PTA used a different Fourier basis set by their own maximum observing time. The semitransparent gray lines are 100 samples from the joint 2D power-law posterior distribution, showing the spread of power-law models that are consistent with all of the PTA's data. Right: 2D posterior for HD-correlated power-law GWB parameters. Contours show 68%, 95%, and 99.7% of the posterior mass. The vertical dotted line is at  $\gamma = 13/3$ .

IPTA, 2309.00693 (ApJ)

## Astro-informed model from

*Siyuan Chen, Alberto Sesana, and Walter Del Pozzo, 1612.00455 (MNRAS)*

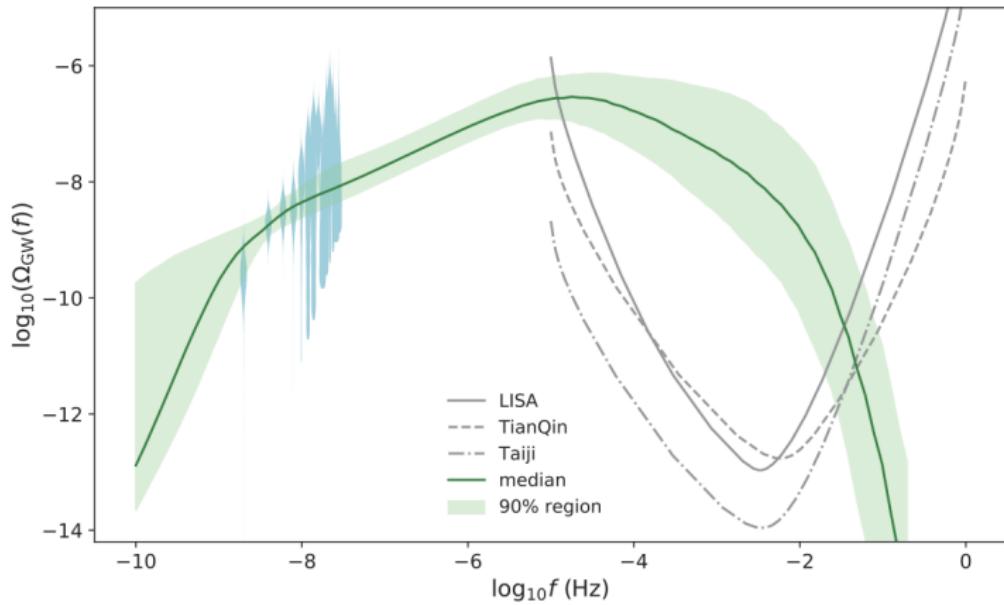
- A large eccentricity when GWs begin to dominate the SMBHB evolution.

*Yan-Chen Bi, Yu-Mei Wu, ZCC, Qing-Guo Huang, 2307.00722 (SCCPMA)*

see also talks from Shao-Jiang Wang and Qing-Juan Yu



# Astro-informed formation model



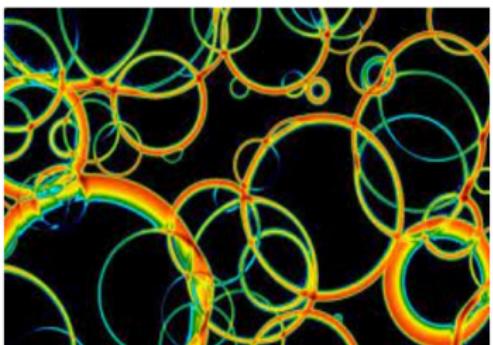
- The SGWB from SMBHBs should be detected by LISA, Taiji and TianQin.

*Yan-Chen Bi, Yu-Mei Wu, ZCC, Qing-Guo Huang, 2307.00722 (SCPMA)*

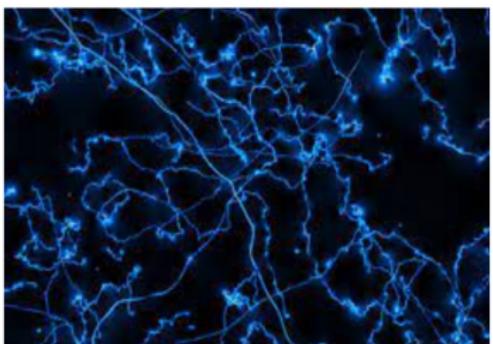
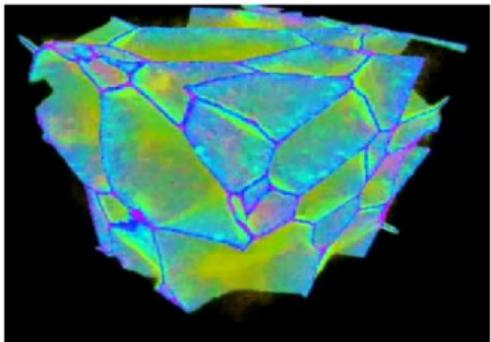


# Cosmological sources

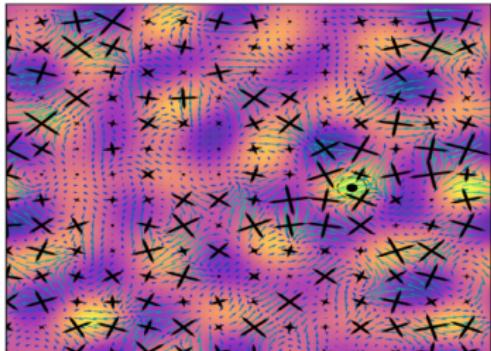
Phase transition



Domain wall



Cosmic string



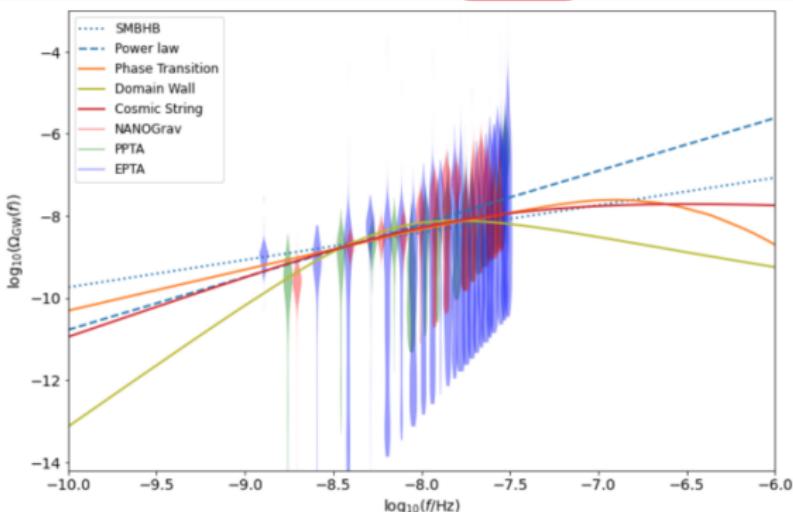
Scalar-induced GW



# Overview of PTA constraints

TABLE II. Bayes factors (BFs) of the power-law (PL), first order phase transition (PT), domain wall (DW), and cosmic string (CS) models compared to the SMBHBs model.

Model	PL	PT	DW	CS
BF	0.569	0.799	0.009	1.699



- Domain wall model is strongly disfavored.



# Phase transition

Bubble collisions + Sound Wave + MHD turbulence  
see also [Shao-Jiang Wang's talk](#)

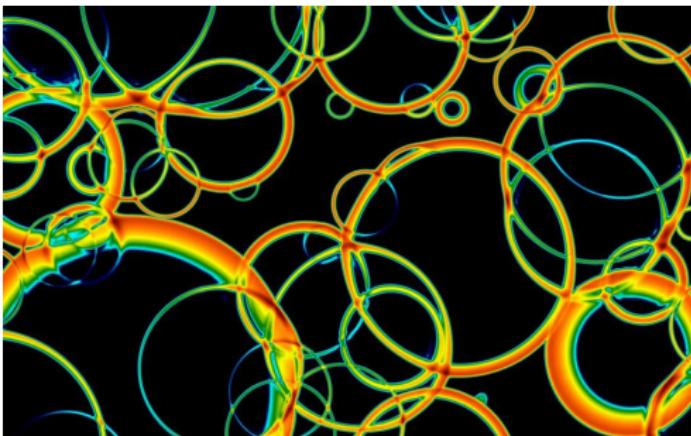
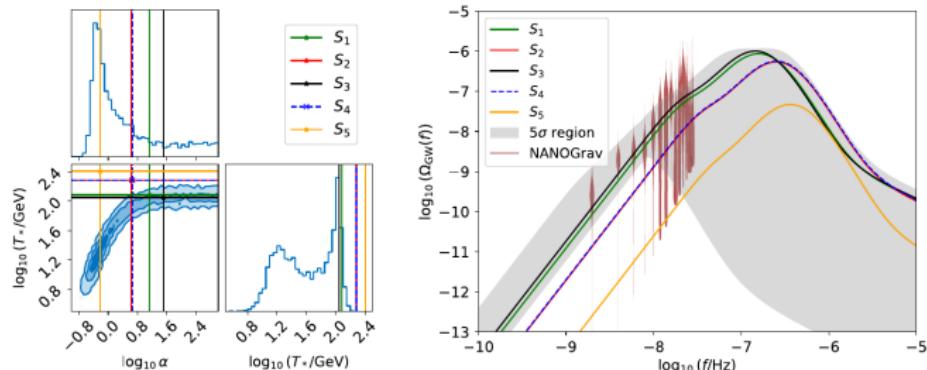


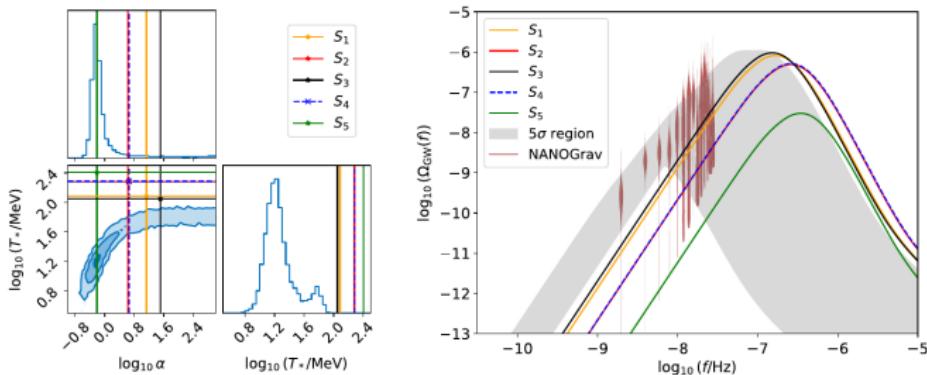
TABLE I. The ratio of the vacuum energy density  $\alpha$  and critical temperature  $T_*$  from five holographical QCD-like models.

Model	QCD matter	Holographic QCD-like model	$\alpha$	$T_*$ (MeV)
$S_1$	Heavy static quarks with a zero chemical potential	Hard wall	13.5	122 [133,144]
$S_2$	Heavy static quarks with a zero chemical potential	Soft wall	4.27	191 [133,144]
$S_3$	Quarks with a finite chemical potential	Hard wall	32.2	112 [134]
$S_4$	Quarks with a finite chemical potential	Soft wall	4.56	192 [134]
$S_5$	Pure gluons	Quenched dynamical holographic QCD	0.611	255 [135]

- Jouguet detonation bubble scenario (a relatively violent PT process)



- nonrunaway bubble scenario (a more gradual and milder PT process)



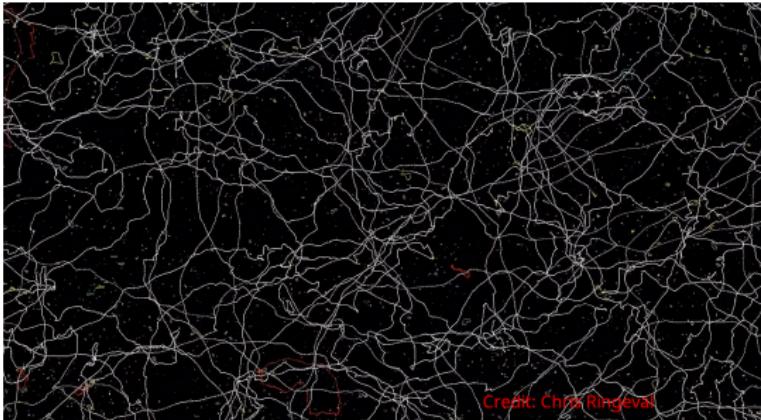
- PTA data prefer pure quark systems under the Jouguet detonations case.

ZCC, Shou-Long Li, Puxun Wu, Hongwei Yu, 2312.01824 (PRD)

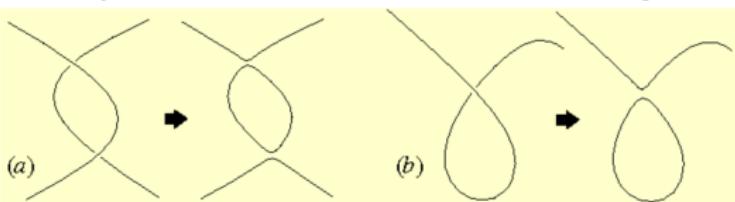


# Cosmic String

- Cosmic strings are linear topological defects that can form in the early Universe from symmetry-breaking phase transitions or be the fundamental strings of superstring theory stretched out to astrophysical lengths.

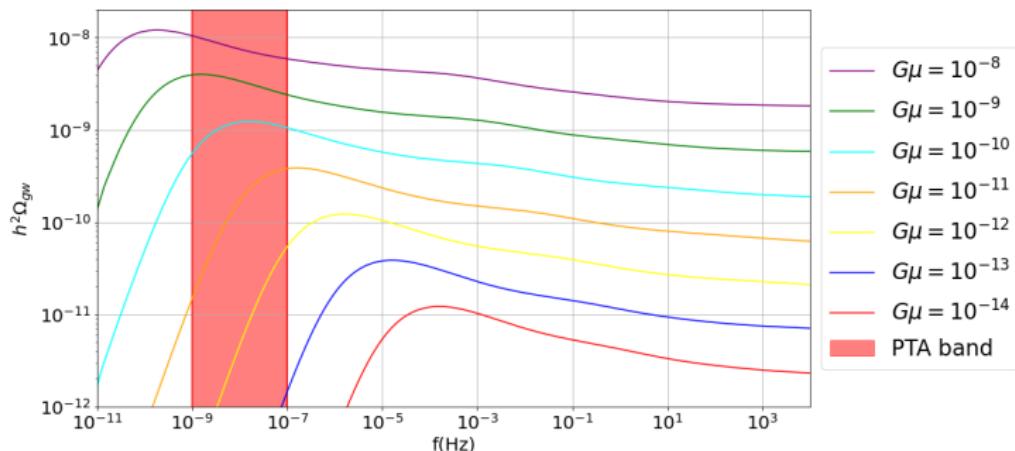


- The intersection between cosmic strings can lead to reconnections and form loops, which will then decay due to relativistic oscillation and emit gravitational waves.





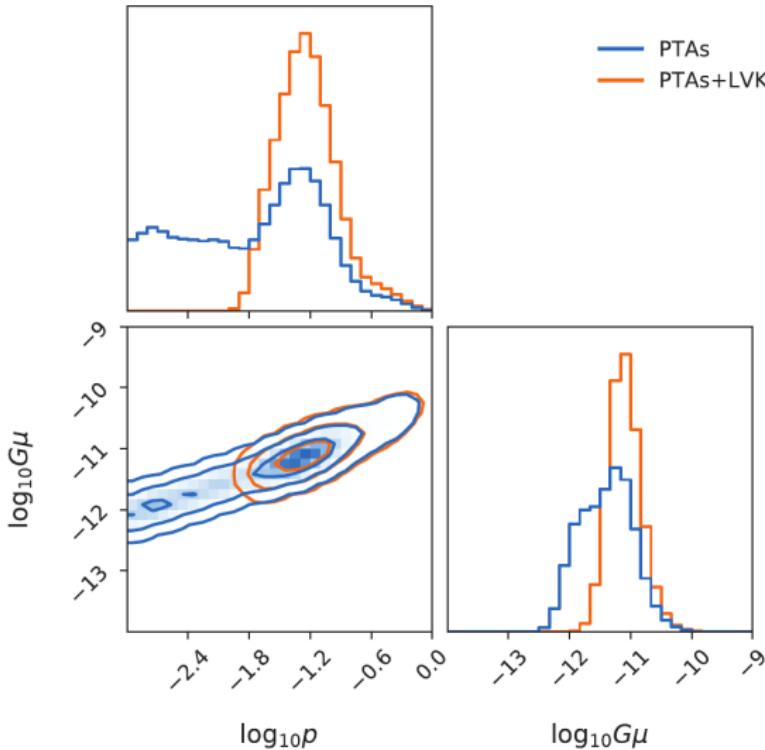
# GW energy density spectrum of cosmic strings



- $G\mu$  is string tension – the energy stored per unit length.
- $p$  is the reconnection probability:
  - $p = 1$  for classical strings
  - $p < 1$  in the string-theory-inspired models



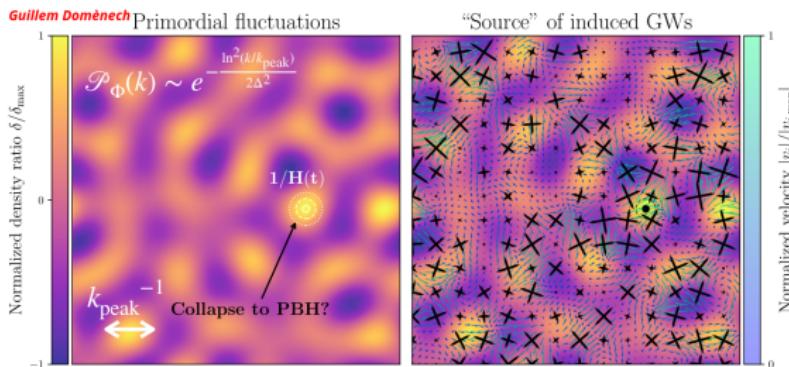
## PE for Cosmic string model



- $p < 1$ : strings in (super) string theory are more likely to explain the detected signal than classical field strings.
- Joint constraints from the LVK O3 data can significantly narrow down the parameter space.



# Scalar-induced GW: see Lang Liu's talk



- Non-Gaussianity of curvature perturbations

*Lang Liu, ZCC, Qing-Guo Huang, 2307.01102 (PRDL)*

- Equation of state and sound speed of the early Universe

*Lang Liu, ZCC, Qing-Guo Huang, 2307.14911 (JCAP)*

*Lang Liu, You Wu, ZCC, 2310.16500 (JCAP)*

- Speed of GW

*ZCC, Jun Li, Lang Liu, Zhu Yi, 2401.09818 (PRDL)*

- Distinguish the adiabatic and isocurvature fluctuations

*ZCC, Lang Liu, 2402.16781*

- Sound speed resonance

*Jia-Heng Jin, ZCC, Zhu Yi, Zhi-Qiang You, Lang Liu, 2307.08687 (JCAP)*



# Summary

$$\langle \tilde{r}_I^*(f) \tilde{r}_J(f') \rangle = \frac{1}{\gamma} \frac{H_0^2}{16\pi^4 f^5} \delta(f - f') \textcolor{red}{\Gamma_{IJ}(f, L_I, L_J, \xi)} \Omega_{\text{gw}}(f)$$

- PTAs have been opening a new window at nHz frequencies.
- Cosmological implications:
  - Domain wall is strongly disfavored.
  - For PT, PTA data prefer pure quark systems under the Jouguet detonations case.
  - Strings in (super)strings theory are more likely to explain the PTA signal than classical field strings.

Thank you for your attention!